



Discriminative Invariant Kernel Features:

A Bells-and-Whistles-Free Approach to Unsupervised Face Recognition and Pose Estimation

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The Problem

Two complementary tasks: To perform two complementary tasks **simultaneously** using a **single unsupervised** feature extractor.

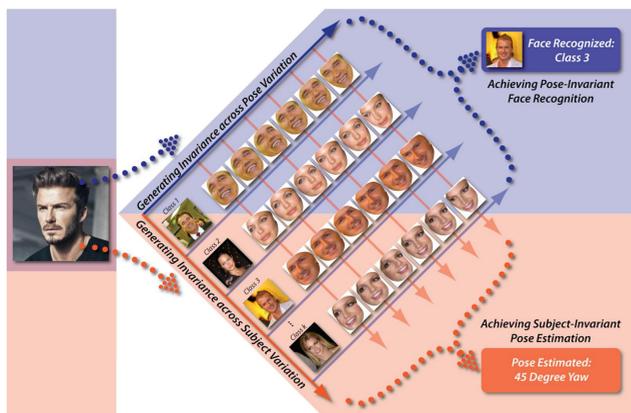


Who is this subject?

What is the subject's pose?

Landmark-free: The paper focuses on **dense landmark-free** (only two eye center locations) face recognition and pose estimation.

Also extends to a completely landmark-free approach which is also **alignment free**.



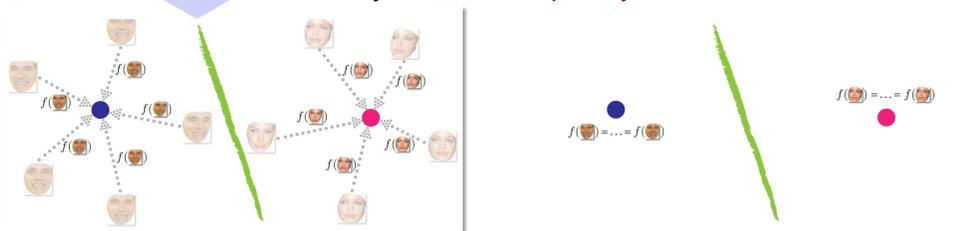
Face recognition sub-feature

Pose estimation sub-feature

The Approach

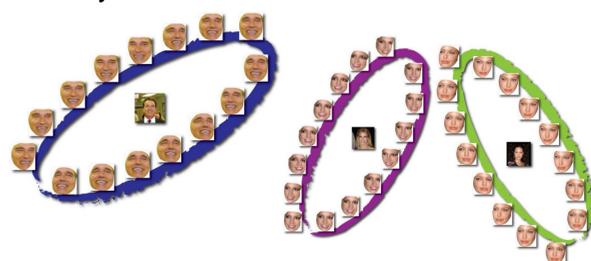
Discriminative Invariant Feature: We extract a **single** highly **discriminative** provably **group invariant non-linear** feature for both tasks from raw pixels.

Invariance to Transformations: Nuisance transformations groups such as the translation, rotation group, **increase complexity** of the learning problem. **Invariance** to such transformations can drastically **reduce complexity**.

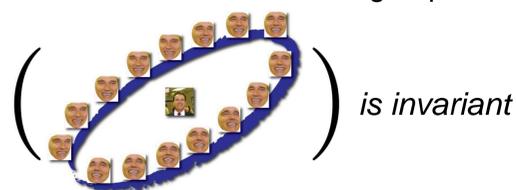


The Approach

Linear Invariant Features: Previous work [1] builds linear invariant that are **implicitly** (but not explicitly) **discriminative**. When a group of transformations act on an object, they create an **orbit**.



The orbit is **unique** to the object, and is an **invariant** to the transformation group

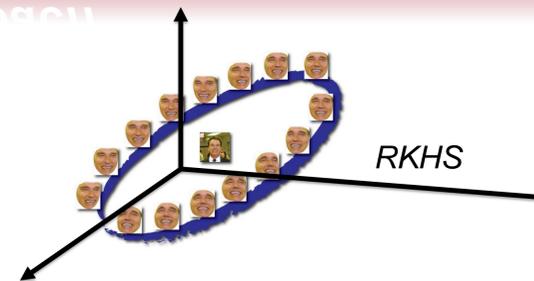


Hence **any measure** of the orbit is an **invariant implicitly discriminative** feature.

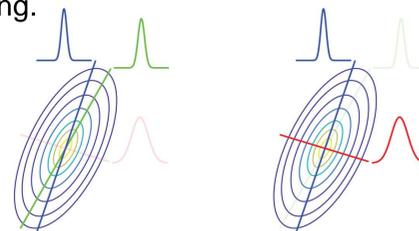


Non-linear Discriminative Invariance: To improve discrimination, we can compute invariant features in the RKHS. We show the **discriminative non-linear** templates form a **group** in the RKHS, leading to Discriminative Invariant Kernel Features.

The Approach



To characterize the orbit, previously simply sampled templates were used. **Explicit** discrimination provides better matching.



Sampled templates Discriminatively learned templates

The **learnt templates** still form a **group** of transformed templates, hence invariance theory holds.

Definition 3.1 (Unitary Kernel). We define a kernel $k(x, y) = \langle \phi(x), \phi(y) \rangle$ to be a unitary kernel if, for a unitary group G , the mapping $\phi(x) : \mathcal{X} \rightarrow \mathbb{H}$ satisfies $\langle \phi(gx), \phi(gy) \rangle = \langle \phi(x), \phi(y) \rangle \forall g \in G, \forall x, y \in \mathcal{X}$.

Theorem 3.2 (DIKF filters form a set of transformed templates in the kernel space under a group). *Given a group G of unitary transformation elements g with $|G| = N$, if $k(x, y) = \langle \phi(x), \phi(y) \rangle$ i.e. k is a unitary kernel, and $\{\mathbf{X}_n \mid \mathbf{X}_n = g_n(\mathbf{X}), g_n \in G\}$ are a set of pre-whitened matrices acted upon by G , then the set of DIKF filters*

$$\mathcal{T}_k = \left\{ \Phi(\mathbf{t}_{kn}) = \Phi(\mathbf{X}_n) (\Phi(\mathbf{X}_n) \cdot \Phi(\mathbf{X}_n))^{-1} \mathbf{u}_k \mid \forall n \right\}$$

is a set of transformed templates under a group.

The Experiments

- Face recognition (153,000 semi-synthetic image dataset):** 1000 subjects with 153 poses each. Images rendered from a 3D model with real texture. We compare DIKF against sampled templates (NDP) and discriminative linear templates (DILF).
- Face recognition (LFW):** Max-pooled DIKF (in red) matches state-of-the-art results on two LFW protocols, despite being simpler than competing methods and working on raw pixels.
- Pose estimation:** 15 poses (-40 to 40 yaw and -20 to 20 pitch, step of 20). Train on the 250 subjects and test on the 1500 images of the remaining 100 subjects.

